



## Review Test Submission: Graded Exam - Unit 7

Course	MAT251: General Calculus II
Test	Graded Exam - Unit 7
Status	Completed
Score	112.5 out of 150 points
Time Elapsed	26 minutes out of 1 hour.
Instructions	

### Question 1

7.5 out of 7.5 points

Consider the sequence

$$a_n = \frac{n}{n^2 + 1}$$

Which of the following are true for this sequence?  
 $\{a_n\}$  is convergent.

Selected Answer:

### Question 2

7.5 out of 7.5 points

$\frac{3}{5} - \frac{3}{6} + \frac{3}{7} - \frac{3}{8} + \dots$  is convergent.

Selected Answer:

### Question 3

7.5 out of 7.5 points

Given that  $a_n > 0$  and  $b_n > 0$  for all  $n$ , and that  $\lim_{n \rightarrow \infty} \frac{a_n}{b_n} = L$ , where  $L \neq 0$  and  $L \neq \infty$ .

Decide whether each of the following are possible according to the Limit Comparison

Test.

$\sum_{n=1}^{\infty} a_n$  converges and  $\sum_{n=1}^{\infty} b_n$  diverges.

Selected Answer:

### Question 4

7.5 out of 7.5 points

A series of the form  $a + ar + ar^2 + \dots + ar^{n-1} + \dots$  is called a \_\_\_\_\_ series.

Selected Answer:

OK

## Question 5

7.5 out of 7.5 points

Given that  $a_n > 0$  and  $b_n > 0$  for all  $n$ , and that  $\lim_{n \rightarrow \infty} \frac{a_n}{b_n} = L$ , where  $L \neq 0$  and  $L \neq \infty$ .

Decide whether each of the following are possible according to the Limit Comparison

Test.

Both  $\sum_{n=1}^{\infty} a_n$  and  $\sum_{n=1}^{\infty} b_n$  converge.

Selected Answer:

## Question 6

0 out of 7.5 points

Find the Maclaurin series for  $f(x) = \frac{x}{1 + \frac{x}{2}}$ .

Selected Answer:

## Question 7

7.5 out of 7.5 points

If  $|r| < 1$ , the series  $a + ar + ar^2 + \dots + ar^{n-1} + \dots$  converges to

Selected Answer:

## Question 8

7.5 out of 7.5 points

The Taylor polynomial of degree  $n$  approximating  $f(x)$  near  $x = a$  is given by:

Selected Answer:

## Question 9

7.5 out of 7.5 points

If  $\sum_{n=1}^{\infty} |a_n|$  is convergent, then is  $\sum_{n=1}^{\infty} a_n$  also convergent.

Selected Answer:

## Question 10

0 out of 7.5 points

A series whose even-numbered terms are positive and odd-numbered terms are negative, or vice versa, is called an \_\_\_\_\_ series.

Selected Answer:

## Question 11

7.5 out of 7.5 points

Find the sum of the series  $-\frac{4}{3} + \frac{4}{3^2} - \frac{4}{3^3} + \frac{4}{3^4} - \dots$  if it exists. Write "diverges" otherwise.

Selected Answer:

## Question 12

0 out of 7.5 points

Consider the sequence

$$a_n = \frac{3^n}{n!}$$

Which of the following are true about  $\{a_n\}$ ?  
 $\{a_n\}$  is monotonic.

Selected Answer:

### Question 13

7.5 out of 7.5 points

A sequence  $\{a_n\}$  converges if

Selected Answer:

### Question 14

7.5 out of 7.5 points

Given that  $0 < a_n \leq b_n$  for all  $n$ , decide whether each of the following statements is true according to the Direct Comparison Test.

If  $\sum_{n=1}^{\infty} b_n$  diverges, then  $\sum_{n=1}^{\infty} a_n$  diverges.

Selected Answer:

### Question 15

0 out of 7.5 points

Find the 50<sup>th</sup> term of the following sequence. Round your answer to the nearest .001 .

$$-\frac{1}{4}, \frac{2}{9}, -\frac{3}{16}, \frac{4}{25}$$

Selected Answer:

### Question 16

7.5 out of 7.5 points

If a series  $\sum_{n=0}^{\infty} a_n(x-c)^n$  converges when  $x$  is in the interval  $[-4, 2]$ , what is the radius of

convergence?

Selected Answer:

### Question 17

7.5 out of 7.5 points

A series of the form  $\sum_{n=0}^{\infty} a_n(x-c)^n$  is called a \_\_\_\_\_ series.

Selected Answer:

### Question 18

0 out of 7.5 points

For which of the following series is the Ratio Test inconclusive (that is, it fails to give a definite answer)?

i.  $\sum_{n=1}^{\infty} \frac{(-1)^n \sqrt{n+1}}{1+n^3}$

ii.  $\sum_{n=1}^{\infty} \frac{1}{n^4}$

iii.  $\sum_{n=1}^{\infty} \frac{(-2)^{n+1}}{\sqrt{n}}$

Selected Answer:

### Question 19

7.5 out of 7.5 points

Consider the sequence

$$\{\ln(n+1) - \ln(n)\}$$

Does the sequence converge or diverge?

If it converges, give its limit. Otherwise write "diverges".

Selected Answer:

### Question 20

7.5 out of 7.5 points

Given that  $0 < a_n \leq b_n$  for all  $n$ , decide whether each of the following statements is true according to the Direct Comparison Test.

If  $\sum_{n=1}^{\infty} b_n$  converges, then  $\sum_{n=1}^{\infty} a_n$  converges.

Selected Answer:

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